

An illustration featuring a central yellow circle with the text "KTUNOTES" in a black, hand-drawn font. The background is a solid blue color. Surrounding the central circle are several hands holding books. In the top left, a hand holds an open book with text. In the top right, a hand holds a closed yellow book. In the bottom left, a hand holds a red book. In the bottom right, a hand holds an open book. In the center bottom, two hands hold a yellow book. To the left of the central circle, there is a stylized graphic of a book with pages fanning out. To the right, there is a stack of books. The overall theme is education and learning.

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MODULE-3

BOTTOM-UP PARSING

General style of bottom-up syntax analysis (bottom up parsing) is shift-reduce parsing. It attempts to construct a parse tree for a input string beginning at leaves (the bottom) and working up towards the root (the top).

This is a process of reducing a string 'w' to the start symbol of the grammar. At each reduction step, a particular step matching right side of production is replaced by the symbol on left side of that production. This process is reverse of right most derivation of a string.

For example, consider the grammar:

$S \rightarrow aABe$

$A \rightarrow Abcb$

$B \rightarrow d$

Derive string abbcde using right most derivation

$S \rightarrow aABe$

$\rightarrow aAde$

$\rightarrow aAbcde$

$\rightarrow abbcde$

$B \rightarrow d$

$A \rightarrow Abc$

$A \rightarrow b$

The string $abcde$ can be reduced to start symbol S by applying following steps

$abcde$

↓

$aAbcde$

↓

$aAde$

↓

$aABe$

↓

S

$A \rightarrow b$

$A \rightarrow Abc$

$B \rightarrow d$

$S \rightarrow aABe$

Thus we can say shift reduce parsing is reverse of right most-derivation of a string.

Handles

is a substring that matches the right-side of a production, and whose reduction to the non-terminal on the left-side of production represent one step along reverse of right most derivation.

Handle pruning

In $\alpha\beta w$, we can use $A \rightarrow \beta$ for reduction. Reducing β to A in $\alpha\beta w$ can be called as handle pruning i.e., removing children of A from parse tree.

STACK IMPLEMENTATION OF SHIFT-REDUCED PARSING

There are 2 problems that must be solved if we are doing parsing by handle pruning.

- (i) has to locate the substring to be reduced in a right sentential form
- (ii) has to determine what production to choose in case there is more than one production with that substring on the right side.

The data structure used to implement shift reduced parsing is stack to hold grammar symbol. In input buffer called string 'w' to be parsed. The symbol '\$' is used to mark bottom of stack and right end of input string. Initially, stack is empty (it contains symbol '\$' only). Initially, input buffer contains string 'w' followed by '\$'. The parser works as follows:

- (i) Parser operates by shifting zero or more input symbol onto the stack until a handle β is on top of stack.
- (ii) Parser then reduces β to the left side of appropriate production.
- (iii) Parser repeats step 1 and 2 until it has detected

an error or until the stack symbol contains the start symbol and input is empty.

Actions made by SRP are:

- (i) shift
- (ii) reduce

(iii) accept

Given error

LR PARSER

LR parsing is an efficient bottom-up syntax analysis technique that can be used to large class of CFG. This technique is also called as

LR(k) parsing



Left to
right scanning
of input

Rightmost
derivation
in reverse.

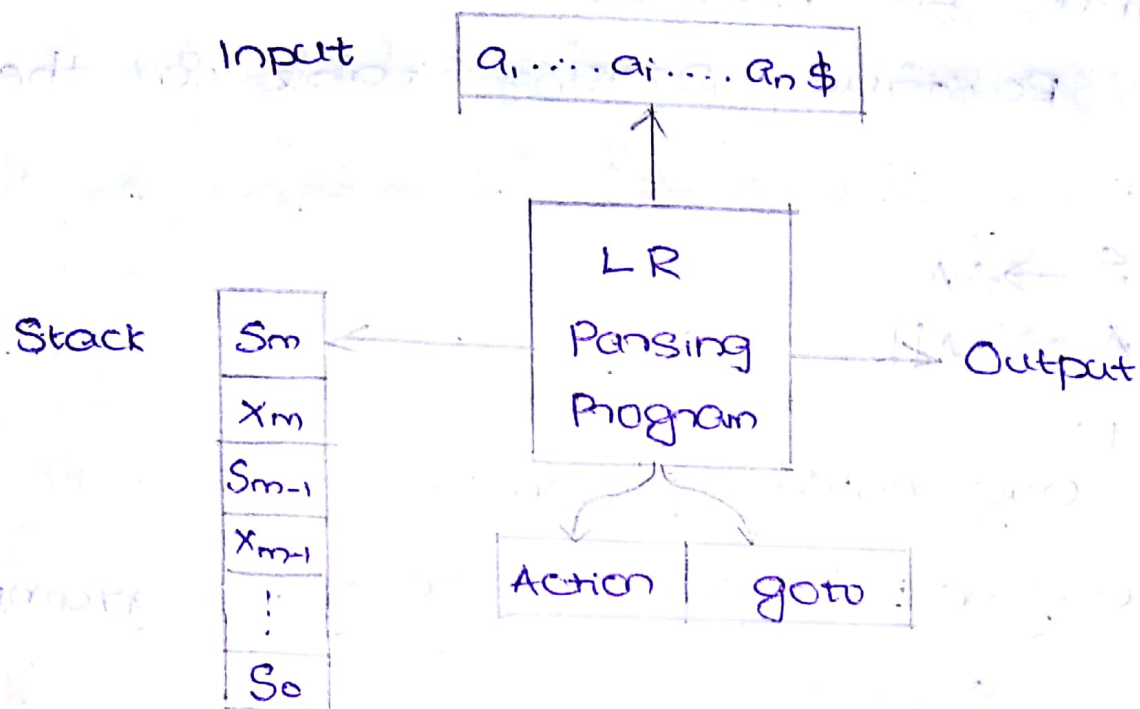
No. of
input symbol
of lookahead.

3 Techniques for constructing LR parsing table for grammar are:

(i) Simple LR (SLR)

(ii) Canonical LR (CLR)

(iii) Lookahead LR (LALR)



For constructing parsing table, the procedure consists of

- (i) LR(k) collection of items to be found.
- (ii) Writing augmented grammar.
- (iii) Defining 2 functions : goto and ~~closure~~ action

AUGMENTED GRAMMAR

If P is a grammar with a start symbol S , then G' , augmented grammar, for G , is G is a grammar with new start symbol S' and a ^{starting} ~~proper~~ production $S \rightarrow S'$. The purpose of this new ^{proper} ~~proper~~ production is to indicate to the parser when it should stop parsing and announce acceptance of input.

SIMPLE LR PARSER

Construct parsing table for the given CFG.

$$S \rightarrow AA$$

$$A \rightarrow aA \mid b$$

Step 1:

Find augmented grammar.

The augmented grammar of given grammar is:

$$S' \rightarrow S$$

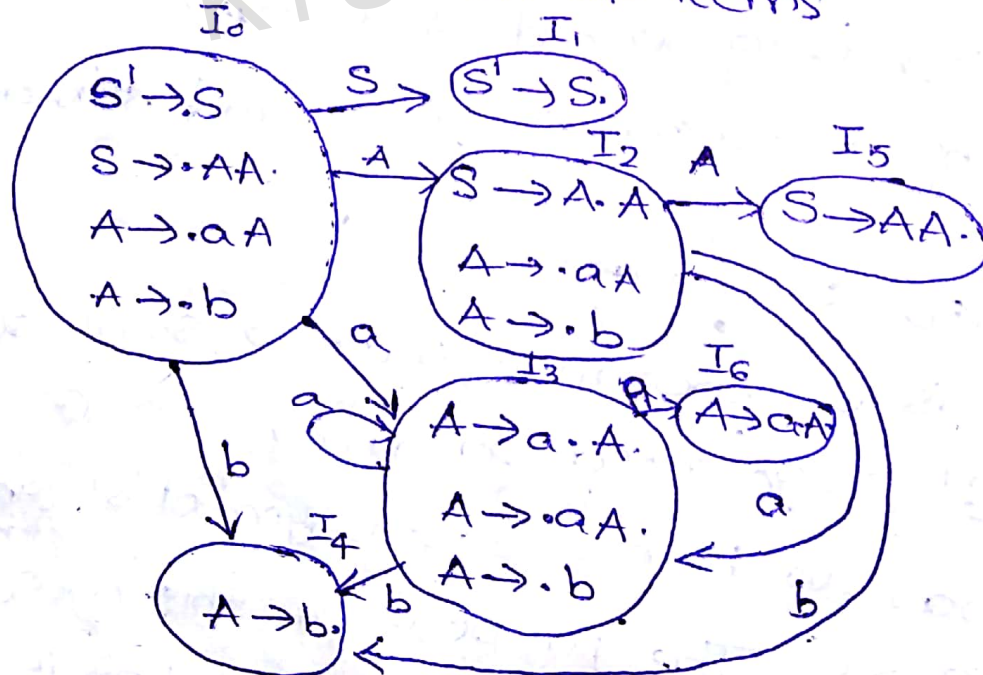
$$S \rightarrow AA$$

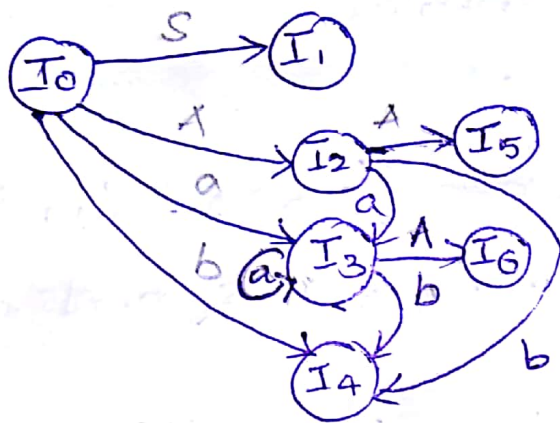
$$A \rightarrow aA \mid b$$

$$A \rightarrow b$$

Step 2:

Find LR(0) collection of items.





The LR(0) collection of items found here are $I_0, I_1, I_2, I_3, I_4, I_5, I_6$

Step 3: Find first and follow of each non-terminal of augmented grammar.

	FIRST	FOLLOW
$S' \rightarrow S$	$\{a, b\}$	$\{\$ \}$
$S \rightarrow AA$	$\{a, b\}$	$\{\$ \}$
$A \rightarrow aA$	$\{a, b\}$	$\{a, b\}, \$ \}$
$A \rightarrow b$	$\{a, b\}$	

Step 4: Construction of parse table. Parse table contains 2 parts (i) Action parts: only for terminal (ii) Goto: only for non-terminal.

	action			goto	
	a	b	\$	A	S
0	S_3	S_4		2	1
1			accept		
2	S_3	S_4		5	
3	S_3	S_4		6	
4	r_3	r_3	r_3		
5	r_1	r_1	r_1		
6	r_2	r_2	r_2		

s_3, s_4 are shift entries

$0, 1, \dots, 6$: States.

r_1, r_2, r_3 : reductions $[S \rightarrow AA \cdot - (1) \text{ in state } 5]$
pop double no. of symbols (here 4)

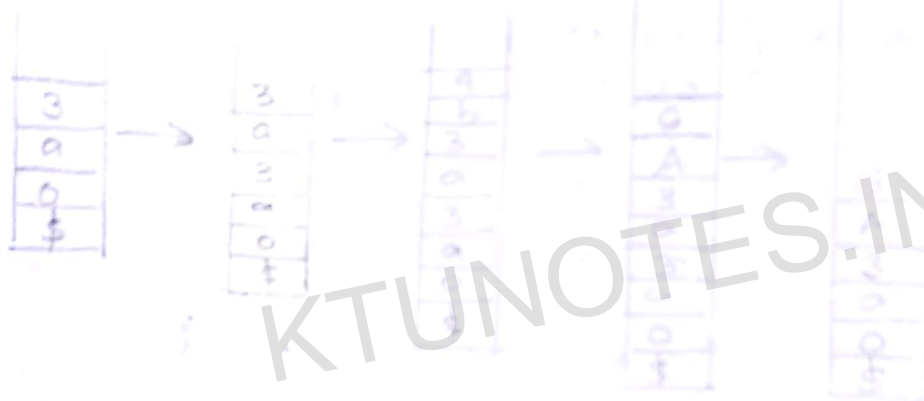
Q Parse the string $aabb\$$ using above given parse table

$aabb\$$

$S \rightarrow AA \cdot (1)$

$A \rightarrow aA \cdot (2)$

$A \rightarrow b \cdot (3)$

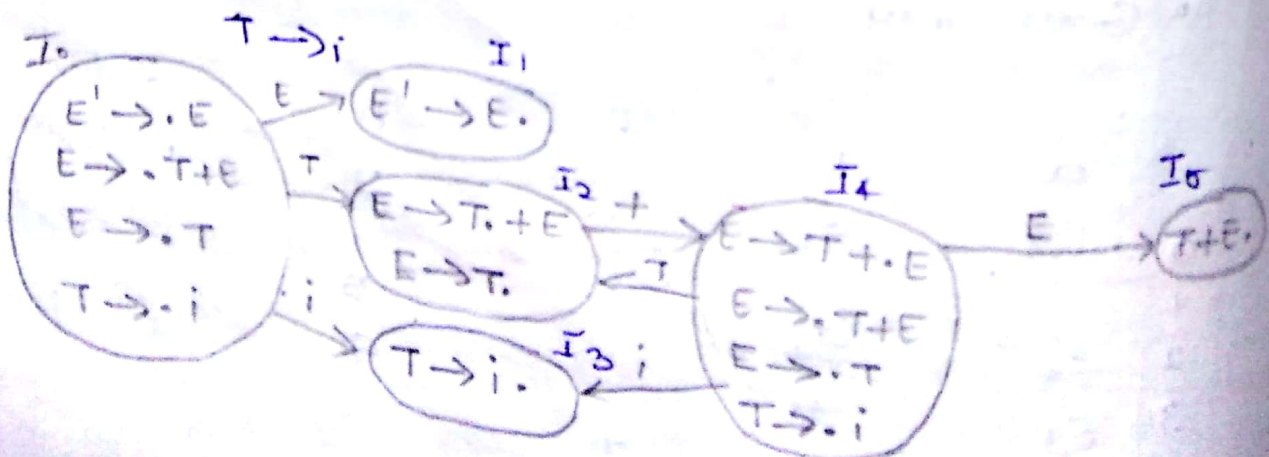


1. Construct a parsing table for grammar.

$E \rightarrow T + E$

$E \rightarrow T$

$T \rightarrow i$



	action			goto	
	i	+	\$	E	T
0	S ₃			1	2
1			accept		
2	r ₂	r ₄	r ₂		
3	r ₃	r ₃	r ₃		
4	S ₃			5	2
5	r ₁	r ₁	r ₁		

$E' \rightarrow E T + E. (1)$

$E \rightarrow T. (2)$

$T \rightarrow i. (3)$

Shift-reduce conflict : When a cell contain both shift and reduce then it has shift-reduce conflict. Then it is not LR(0).

LL(1) should not contain left recursive.

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CONFLICT DURING

There are CFGs for which shift reduce parsing cannot be used. The 2 types of conflict

(i) shift/reduce

(ii) cannot decide whether to shift or reduce

(iii) reduce/reduce

: cannot decide which of the several reduction to make.

CANONICAL LR(1) COLLECTION OF ITEMS

In LR(0) parsing table, there is a chance for shift-reduced conflict because we are entering

'reduce' corresponding to all the states which are terminating states. We can solve this problem by entering 'reduce' corresponding to the follow of LHS of the production in the terminating state. This is called SLR(1) collection of items

	FIRST	FOLLOW
$E \rightarrow T + E$	$\{i\}$	$\{\$, \}$
$E \rightarrow T$	$\{i\}$	
$T \rightarrow i$	$\{i\}$	$\{+, \$ \}$

Parsing table

	action			goto	
	i	+	\$	E	T
0	S ₃			1	2
1			accept		
2		S ₄	r ₂		
3		r ₃	r ₃		
4	S ₃			5	2
5			r ₁		

Q $S \rightarrow dA|aB$
 $A \rightarrow bA|c$
 $B \rightarrow bB|c$

Check whether it is LL(1), LR(0), SLR(1)

$S \rightarrow dA|aB$

$A \rightarrow bA|c$

$B \rightarrow bB|c$

FIRST

FOLLOW

$S \rightarrow dA|aB$

$\{d, a\}$

$\{\$, \}$

$A \rightarrow bA|c$

$\{b, c\}$

$\{d\}$

$B \rightarrow bB|c$

$\{b, c\}$

$\{\$, \}$

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$S' \rightarrow S$

$S \rightarrow dA|aB$

$B \rightarrow bB|c$

$A \rightarrow bA|c$

$S' \rightarrow S$

$S' \rightarrow S$

$S \rightarrow dA$

$S \rightarrow aB$

$A \rightarrow bA$

$A \rightarrow c$

$B \rightarrow bB$

$B \rightarrow c$

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MORE POWERFUL LR PARSERS.

In this section, we shall extend the previous LR parsing techniques to use one symbol of look ahead on the input. There are 2 different methods

- (i) Canonical LR Parser (CLR)
- (ii) LALR Parser.

CLR

The Canonical LR method which makes full use of lookahead symbol this method uses large set of items called LR(1) items.

LALR

which is based LR(0) collection of items and has ^{many} few space than typical parsers based on LR(1) items. Large class of grammars can be handled using LALR method. LALR method is most powerful one.

Canonical LR(1) items.

$S \rightarrow AA$

$A \rightarrow aA$

$A \rightarrow b$

$S \rightarrow S, \$$

$S \rightarrow \cdot AA, \$$

$\$$ closure of S : $S \rightarrow \cdot AA$

$\$$ first of $\$$

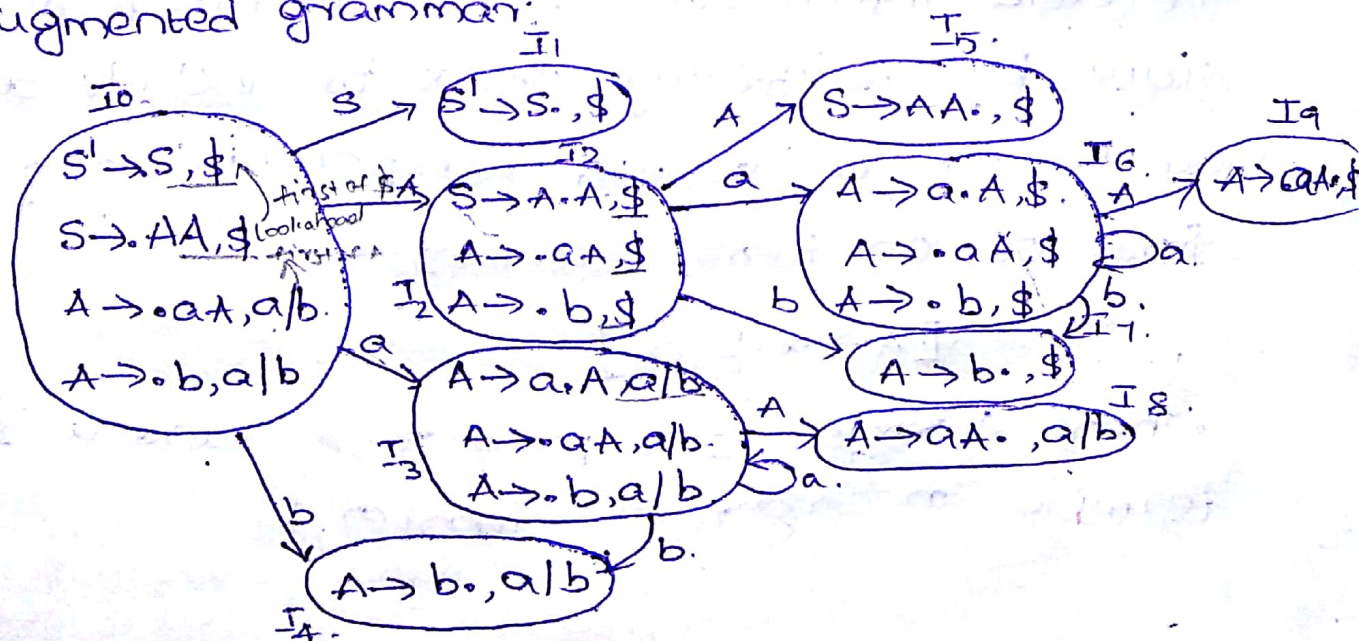
$A \rightarrow \cdot aA, a/b$

a closure of A : $A \rightarrow \cdot aA$

a/b first of A

We can construct CLR(1) items as follows:

Augmented grammar:



	Action			goto	
	a	b	\$	A	S
0	S ₃	S ₄		2	1
1			accept		
2	S ₆	S ₁		5	
3	S ₃	S ₄		8	
4	r ₃	r ₃			
5			r ₁		
6	S ₆	S ₄		9	
7			r ₃		
8	r ₂	r ₂			
9			r ₂		

It
 $S \rightarrow AA \cdot \$$

↓
 thus r₁ in \$

$S \rightarrow AA \cdot (1)$

$A \rightarrow aA \cdot (2)$

$A \rightarrow b \cdot (3)$

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IF LR(0) and LR(1) collection of items, we are only considering the productions, it is possible to carry more information in state, that will allow us to rule out some of the invalid reductions. The extra information is incorporated into the state by redefining items to include a terminal symbol as a second component. The general form of an item becomes:

$$[A \rightarrow \alpha \cdot \beta, a]$$

where $A \rightarrow \alpha \beta$, is a production and a is a terminal or right end marker \$.

This object can be called as LR(1) items.
In LR(1) the digit 1 refers the length of the second component, called the lookahead of the item.

LALR PARSING

Consider the grammar,

$S \rightarrow AA$

$A \rightarrow aA$

$A \rightarrow b$

and also consider CLR parsing table which is given in the last example.

	Action		Goto	
	a	b	A	\$
0	S ₃₆	S ₄₇	2	1
1	accept			
2	S ₃₆	S ₄₇	5	
36	S ₃₆	S ₄₇	89	
47	r ₃	r ₃		
5	.		r ₁	
86	S ₃₆	S ₄₇	89	
47			r ₃	
89	r ₂	r ₂		
89			r ₂	

	Action			Goto	
	a	b	\$	A	\$
0	S ₃₆	S ₄₇		2	1
1	accept				
2	S ₃₆	S ₄₇		5	
36	S ₃₆	S ₄₇		89	
47	r ₃	r ₃	r ₃		
5			r ₁		
89	r ₂	r ₂	r ₂		